



# Dielectronic Recombination in Pb78+ Near the Ionization Threshold

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**ABSTRACT:** Semi-relativistic perturbation theory calculations are carried out for dielectronic recombination cross sections involving the  $1s^22s2pnl$  subshells of  $Pb^{77+}$  as found above the  $Pb^{78+}$   $1s^22s^2$  ionization threshold. We included levels in the  $1s^22s2pnl$  subshells of  $Pb^{77+}$  for n=7-20 and l=0-4. Theoretical dielectronic recombination cross sections are presented for the  $1s^22s2p19l$  subshells of  $Pb^{77+}$  to compare with planned experimental dielectronic recombination measurements at CRYRING.

#### 1. INTRODUCTION

Resonance states near the ionization threshold may contribute to dielectronic recombination in astrophysical and laboratory plasmas[1, 2]. Recently dielectronic recombination has been observed in electron collisions with highly charged atomic ions in the synchrotron storage ring CRYRING[3] in the FAIR complex in Darmstadt, Germany[4].

In this paper semi-relativistic perturbation theory calculations are made for dielectronic recombination cross sections involving the 1s<sup>2</sup>2s2pnl subshells of Pb<sup>77+</sup> lying above the the Pb<sup>78+</sup> 1s<sup>2</sup>2s<sup>2</sup> ionization threshold. Theoretical dielectronic recombination cross sections are presented for the 1s<sup>2</sup>2s2p19l subshells of Pb<sup>77+</sup> to compare with future experimental dielectronic recombination measurements[5].

The rest of the paper is structured as follows: in section 2 we review theory, in section 3 we present results, and in section we give a brief summary. Unless otherwise stated, all quantities are given in atomic units.

#### 2. THEORY

The dielectronic recombination cross section for an N electron ground level with statistical weight  $g_i$  combining into an (N+1) electron doubly excited level with statistical weight  $g_i$  is given by [6]:

$$\sigma_{i \to j} = \frac{\pi^2}{E_c \Delta E_c} \frac{g_j}{2g_i} A_a(j \to i) B_j \tag{1}$$

where  $E_c$  is the energy of the continuum electron and  $\Delta E_c$  is bin width. The branching ratio for radiative stabilization is given by:

$$B_j = \frac{\sum_n A_r(j \to n)}{\sum_k A_a(j \to k) + \sum_n A_r(j \to n)} , \tag{2}$$

where the radiative rate is given by:

$$A_r(j \to n) = 2\pi |\langle n|D|j \rangle|^2$$
, (3)

where D is the dipole radiation field operator, and the autoionization rate is given by:

$$A_a(j \to n) = 4/k| < n|V|j > |^2$$
, (4)

where V is the electrostatic interaction between electrons. The electron linear momentum is taken as  $k = \sqrt{2|E_{jn}|}$  for the evaluation of the autoionization rates.

Dielectronic recombination cross sections are calculated using a configuration-average distorted-wave (CADW) approximation[7]. The bound state wavefunctions and energies employed in the CADW calculations are calculated in a semi-relativistic Hartree-Fock approximation[8].

## 3. PLANNED EXPERIMENT

The CRYRING[3] in the FAIR complex in Darmstadt, Germany[4] is a magnetic heavy ion storage ring. Ions are kept in orbit with 12 dipole magnets connected by 12 straight sections. There are 6 straight sections that implement beam focusing, while the additional 6 straight sections are interleaved that provide ion injection, electron cooling, ion extraction, and diagnostics. Heavy metals like Ta, W, Pb, and U are studied at CRYRING to better understand their atomic collision properties.

#### 4. THEORETICAL RESULTS

Semi-relativistic autoionization rate calculations were carried out for the 70 1s<sup>2</sup>2s2pnl n = 7 - 20 1 = 0 - 4 subshells of Pb<sup>77+</sup> that lie above the 1s<sup>2</sup>2s<sup>2</sup> ionization threshold of Pb<sup>78+</sup>. Semi-relativistic radiative rate calculations were carried out for the decay of the 70 subshells to the 17 1s<sup>2</sup>2s2pnl n = 3 - 61 = 0 - 4 subshells of Pb<sup>77+</sup> that lie below the 1s<sup>2</sup>2s<sup>2</sup> ionization threshold of Pb<sup>78+</sup>. Using a bin width of  $\Delta E_c = 5.44$  eV the cross sections are presented in Figure 1 over an energy range from 0.0 eV to 2000.0 eV. Simple extrapolations were made to n = 1000 and 1 = 12 for the cross sections.

Semi-relativistic radiative rate calculations were also carried out for the decay of the 70 subshells to the  $17 \cdot 1s^2 2s^2 pnl \cdot n = 3 - 61 = 0 - 4$  subshells and the  $70 \cdot 1s^2 2s^2 nl \cdot n = 7 - 201 = 0 - 4$  subshells of  $Pb^{77+}$  that lie below the  $1s^2 2s^2$  ionization threshold of  $Pb^{78+}$ . With only a 2% increase in the radiative rates there was little change in the cross sections as presented in Figure 1.

To compare with future experiments semi-relativistic autoionization rate calculations were carried out for the 5  $1s^22s2p1911=0$  - 4 subshells of Pb<sup>77+</sup>. Semi-relativistic radiative rate calculations were carried out for the decay of the 5 subshells to the 17  $1s^22s2pn1$  n = 3 - 61 = 0 - 4 subshells of Pb<sup>77+</sup> that lie below the  $1s^22s^2$  ionization threshold of Pb<sup>78+</sup>. Using a bin width of  $\Delta E_c = 0.27$  eV the cross sections are presented in Figure 2 over an energy range from 1670.0 eV to 1690.0 eV.

#### 5. SUMMARY

Semi-relativistic perturbation theory has been applied to calculate the dielectronic recombination in Pb<sup>78+</sup>. To compare with future experiments, semi-relativistic dielectronic recombination cross sections in Pb<sup>78+</sup> near the ionization potential involving the Pb<sup>77+</sup>  $1s^22s2pnl$  n = 19 l = 0 - 4 states were calculated. In the future we plan to make more dielectronic recombination cross section calculations for highly charged atomic ions to compare with experiment.

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